

# Notes: DILATIONS

**Content Objective:** *I will be able to apply a scale factor to a preimage to create an enlargement or reduction on a coordinate plane.*

TERM	DESCRIPTION	EXAMPLE
Dilation	A transformation that produces a similar figure by either enlarging or reducing the original figure by a scale factor, $k$ .	
	A fixed point about which the preimage is enlarged or reduced,	Usually the origin, $(0,0)$
Scalar	A number, represented by the variable $k$ , used as a multiplier in scaling. The ratio of the image to the preimage.	$\frac{\text{IMAGE}}{\text{PREIMAGE}}$
enlargement	A dilation with a scale factor greater than 1; the image is larger than the preimage.	$k > 1$
reduction	A dilation with a scale factor greater than 0 but less than 1; the image is smaller than the preimage.	$0 < k < 1$
	When the scale factor of 1 is applied the preimage and the image are the same shape and the same size.	$k = 1$

## COORDINATE RULES FOR DILATIONS

**When a point  $P(a, b)$  is dilated by a scale factor  $k$ , then the following rules apply to the coordinates:**

$$P(a, b) \rightarrow P'(ka, kb)$$

Use the given scale factor and center to dilate the figures and state the new coordinates. Graph the image.

**EXAMPLE 1**

Scale Factor:  $\frac{1}{2}$ ; Center:  $(0,0)$

S' (\_\_\_\_, \_\_\_\_)

T' (\_\_\_\_, \_\_\_\_)

R' (\_\_\_\_, \_\_\_\_)

S (-3, 6)

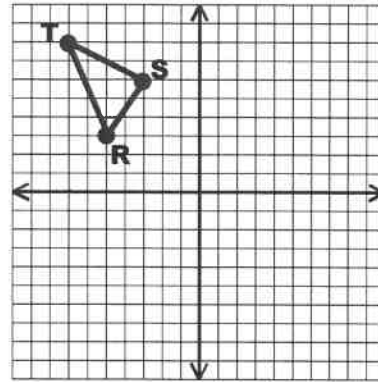
S' (-1.5, 3)

T (-7, 8)

T' (-3.5, 4)

R (-5, 3)

R' (-2.5, 1.5)



(1) Find  $\frac{1}{2}$  of each coordinate.

(2) The "preimage" is  $\triangle STR$ . After the dilation (which was a reduction) the "image" is  $\triangle S'T'R'$

\* original figure:  $\triangle STR$   
 New figure:  $\triangle S'T'R'$   
 $K = \frac{1}{2}$ ; reduction

**EXAMPLE 2:**

Scale Factor: 3; Center: Origin

M' (\_\_\_\_, \_\_\_\_)

N' (\_\_\_\_, \_\_\_\_)

O' (\_\_\_\_, \_\_\_\_)

M (1, -2)

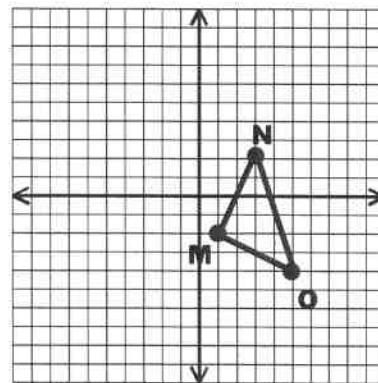
M' (3, -6)

N (3, 2)

N' (9, 6)

O (5, -4)

O' (15, -12)



1) Find 3 times each coordinate

2) The "pre image" is  $\triangle MNO$ . The "image" is  $\triangle M'N'O'$ , which is an enlargement.

\* original figure:  $\triangle MNO$   
 New figure:  $\triangle M'N'O'$   
 $K = 3$ ; enlargement